

A deep-learning method for precipitation nowcasting

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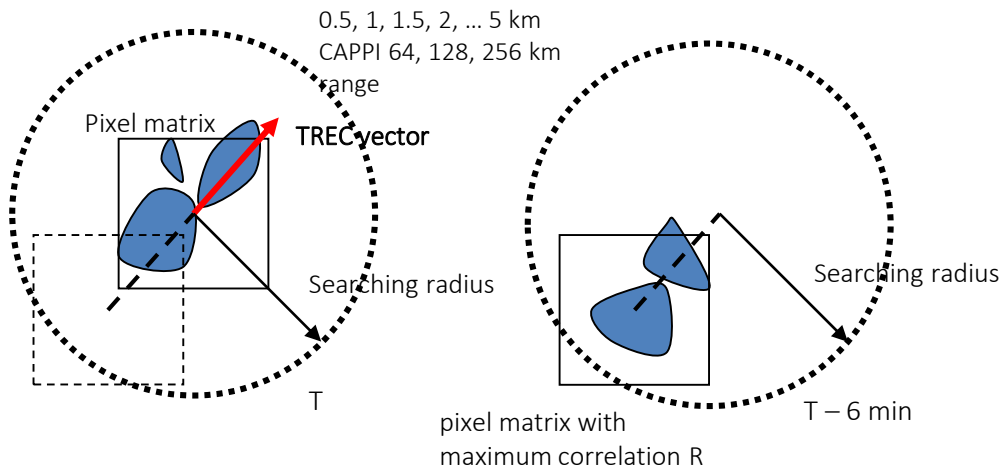
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Echo Tracking in SWIRLS Radar Nowcasting System

- Maximum Correlation (TREC)



where Z_1 and Z_2 are the reflectivity at T+0 and T+6min respectively

$$R = \frac{\sum_k Z_1(k) \times Z_2(k) - \frac{1}{N} \sum_k Z_1(k) \sum_k Z_2(k)}{\left[\left(\sum_k Z_1^2(k) - N \bar{Z}_1^2 \right) \times \left(\sum_k Z_2^2(k) - N \bar{Z}_2^2 \right) \right]^{1/2}}$$

- Optical Flow

MOVA – Multi-scale Optical-flow by Variational Analysis

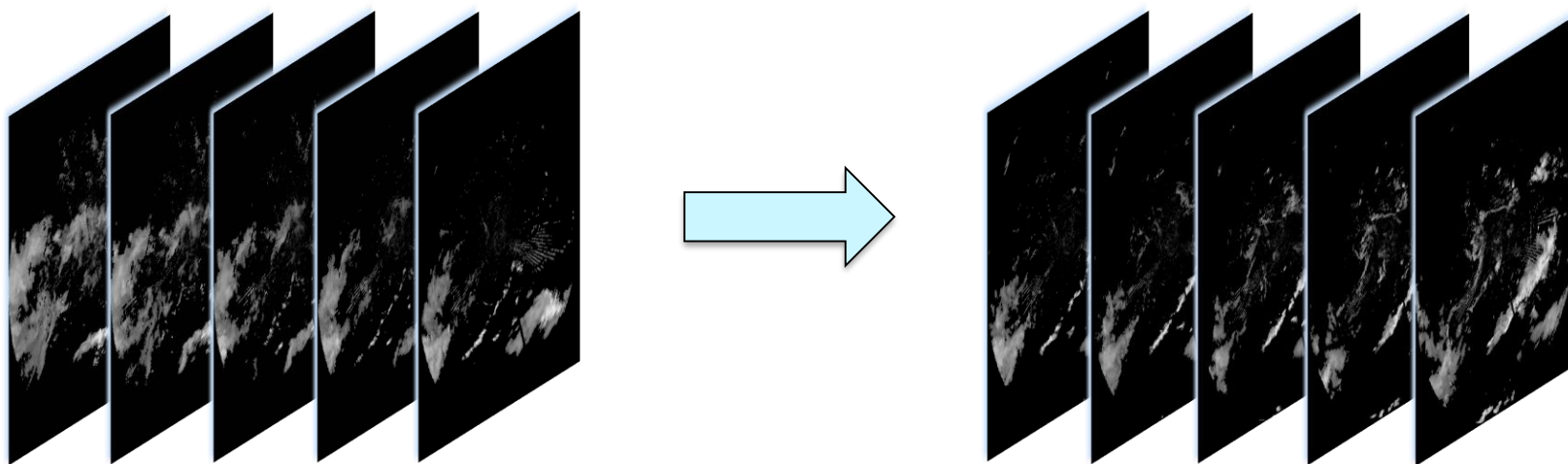
ROVER – Real-time Optical-flow by Variational method for Echoes of Radar

Given $I(x,y,t)$ the image brightness at point (x,y) at time t and the brightness is constant when pattern moves, the echo motion components $u(x,y)$ and $v(x,y)$ can be retrieved via minimization of the cost function:

$$J = \iint \left[\frac{\partial I}{\partial t} + u \frac{\partial I}{\partial x} + v \frac{\partial I}{\partial y} \right]^2 dx dy$$

Predicting evolution of weather radar maps

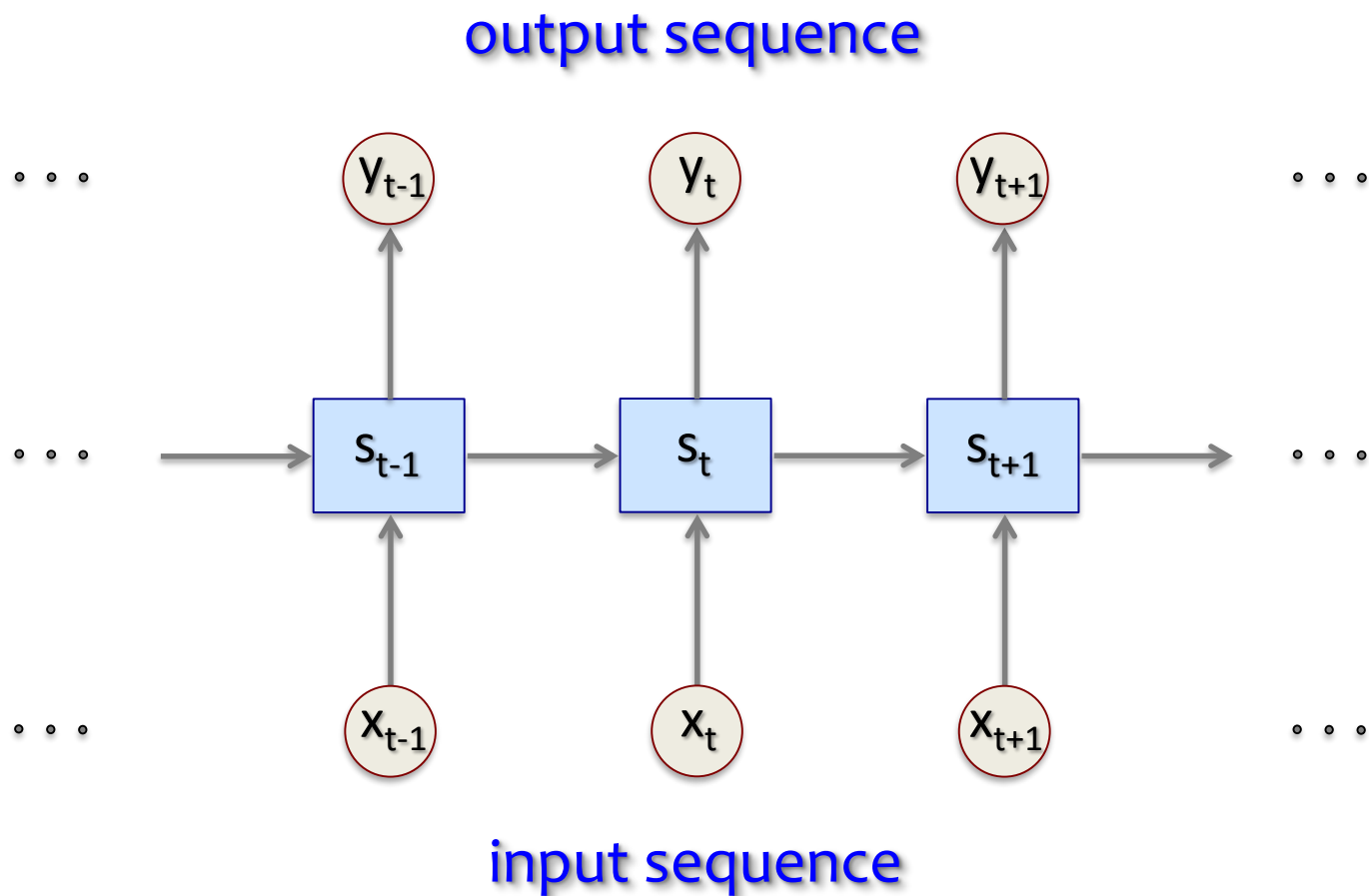
- **Input sequence:** observed radar maps up to current time step
- **Output sequence:** predicted radar maps for future time steps



$$\tilde{\mathcal{X}}_{t+1}, \dots, \tilde{\mathcal{X}}_{t+K} = \arg \max_{\mathcal{X}_{t+1}, \dots, \mathcal{X}_{t+K}} p(\mathcal{X}_{t+1}, \dots, \mathcal{X}_{t+K} \mid \hat{\mathcal{X}}_{t-J+1}, \hat{\mathcal{X}}_{t-J+2}, \dots, \hat{\mathcal{X}}_t)$$

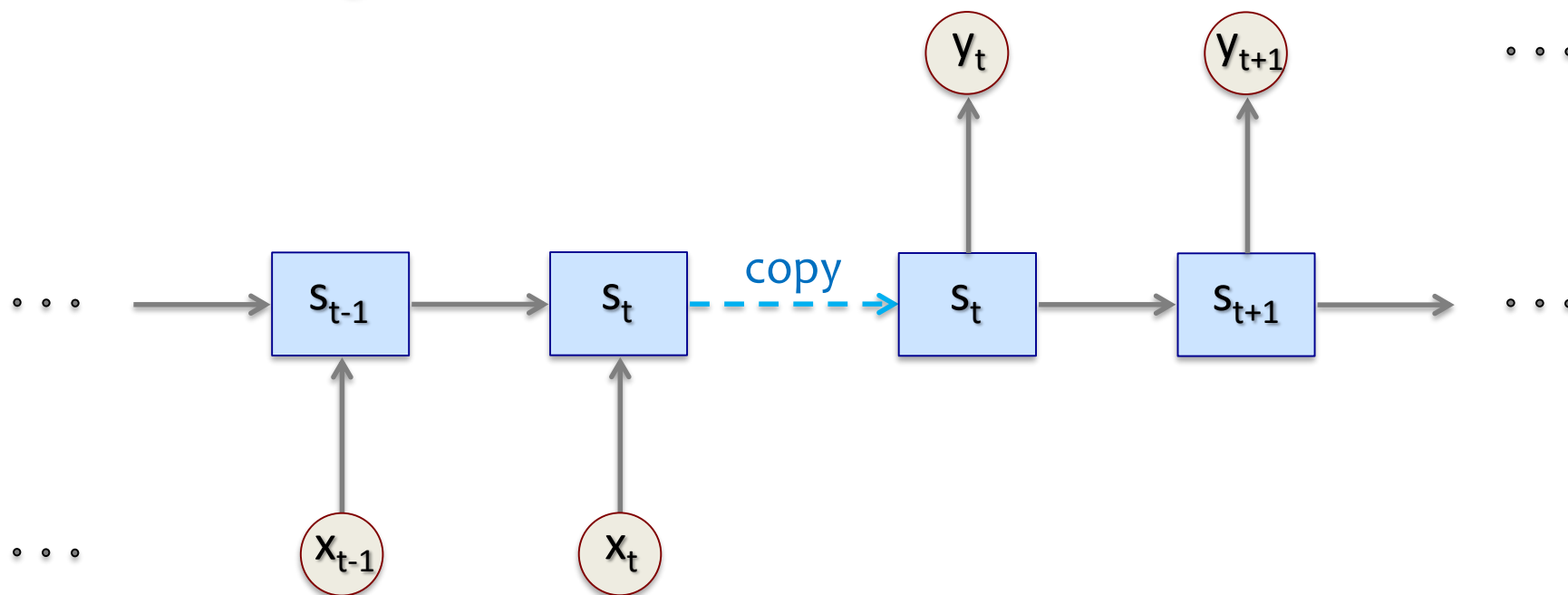
Maximize posterior pdf of echo sequence across K time levels based on previous J time levels of observations

Sequence-to-sequence learning



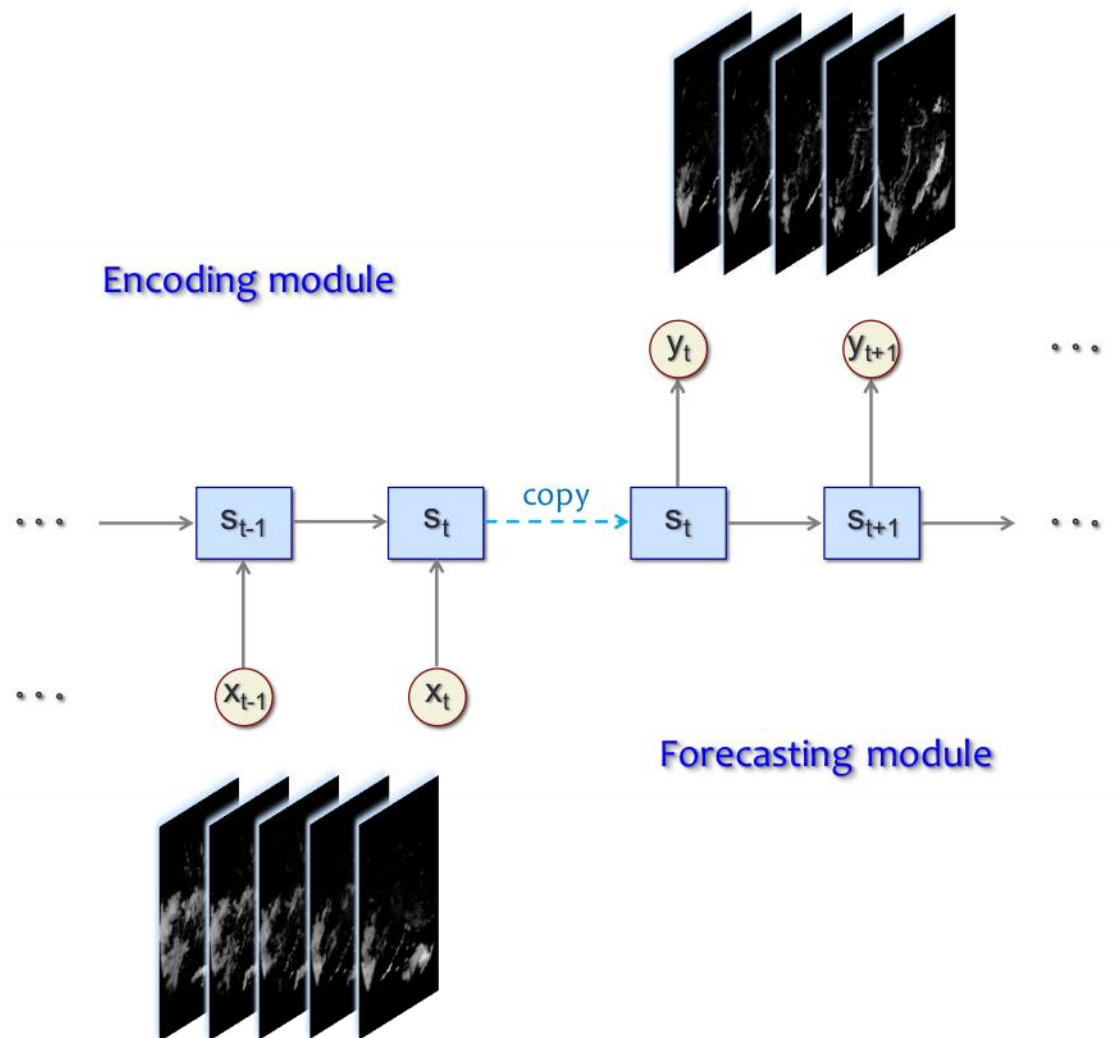
Encoding-forecasting model

Encoding module



Forecasting module

Spatiotemporal encoding-forecasting model



ConvLSTM model

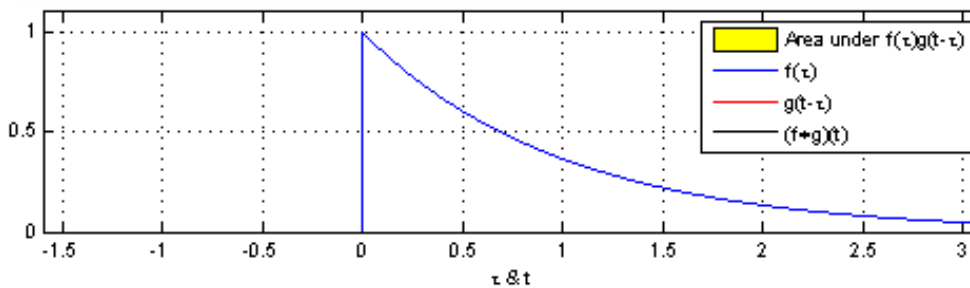
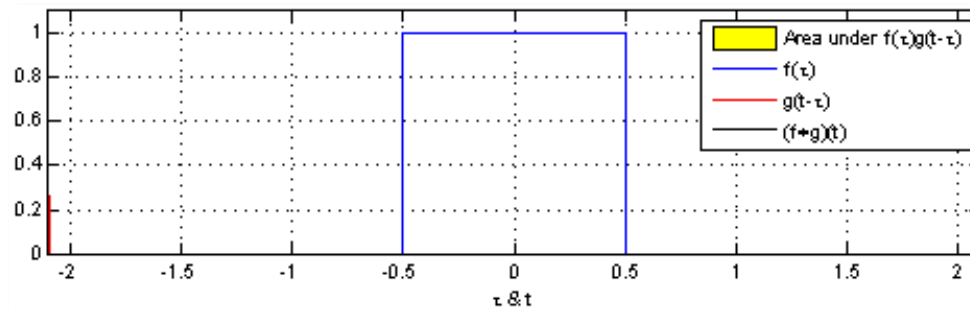
- Convolutional long short-term memory (ConvLSTM) model

X. Shi, Z. Chen, H. Wang, D.Y. Yeung, W.K. Wong, and W.C. Woo. Convolutional LSTM network: A machine learning approach for precipitation nowcasting. *NIPS 2015*.

- Two key components:
 - Convolutional layers
 - Long short-term memory (LSTM) cells in recurrent neural network (RNN) model

Convolution

- An operation on **two functions**
- Produces a third function which gives the **overlapped area** of the two functions as a function of the translation of one of the two functions



Convolution

- **Continuous** domains:

$$(f * g)(t) = \int_{-\infty}^{\infty} f(\tau) g(t - \tau) d\tau = \int_{-\infty}^{\infty} f(t - \tau) g(\tau) d\tau = (g * f)(t)$$

- **Discrete** domains:

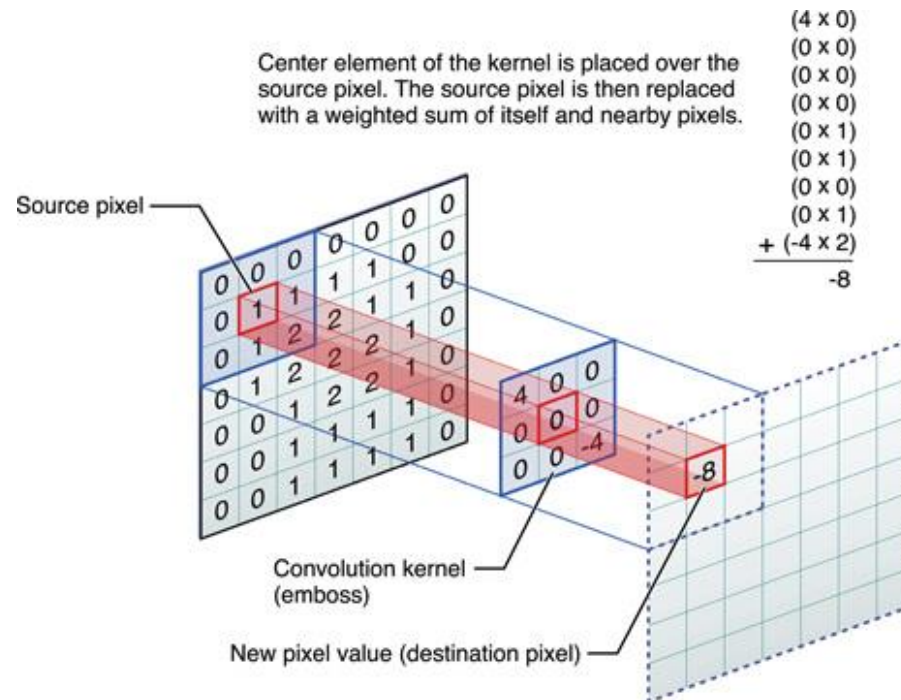
$$(f * g)[n] = \sum_{m=-\infty}^{\infty} f[m] g[n - m] = \sum_{m=-\infty}^{\infty} f[n - m] g[m] = (g * f)[n]$$

- **Discrete** domains with **finite support**:

$$(f * g)[n] = \sum_{m=-M}^M f[n - m] g[m]$$

2D convolution

- 2D convolution (a.k.a. **spatial convolution**) as **linear spatial filtering**



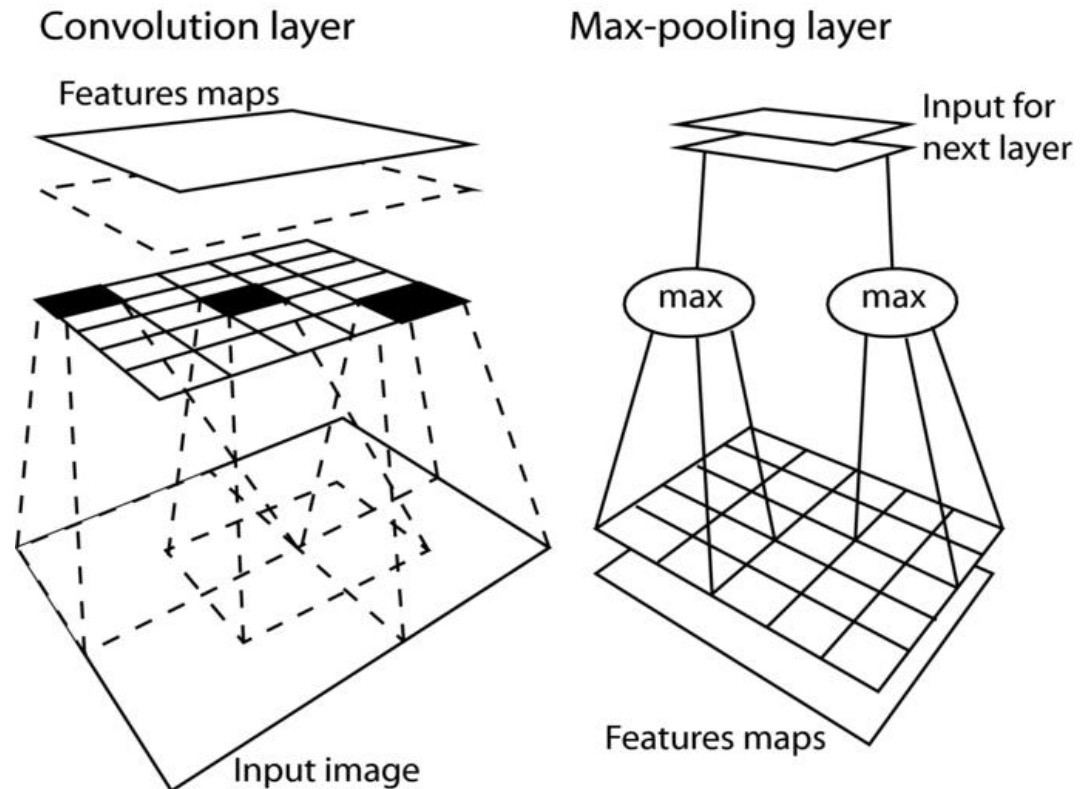
- Multiple **feature maps**, one for each convolution operator

Convolutional and pooling layers

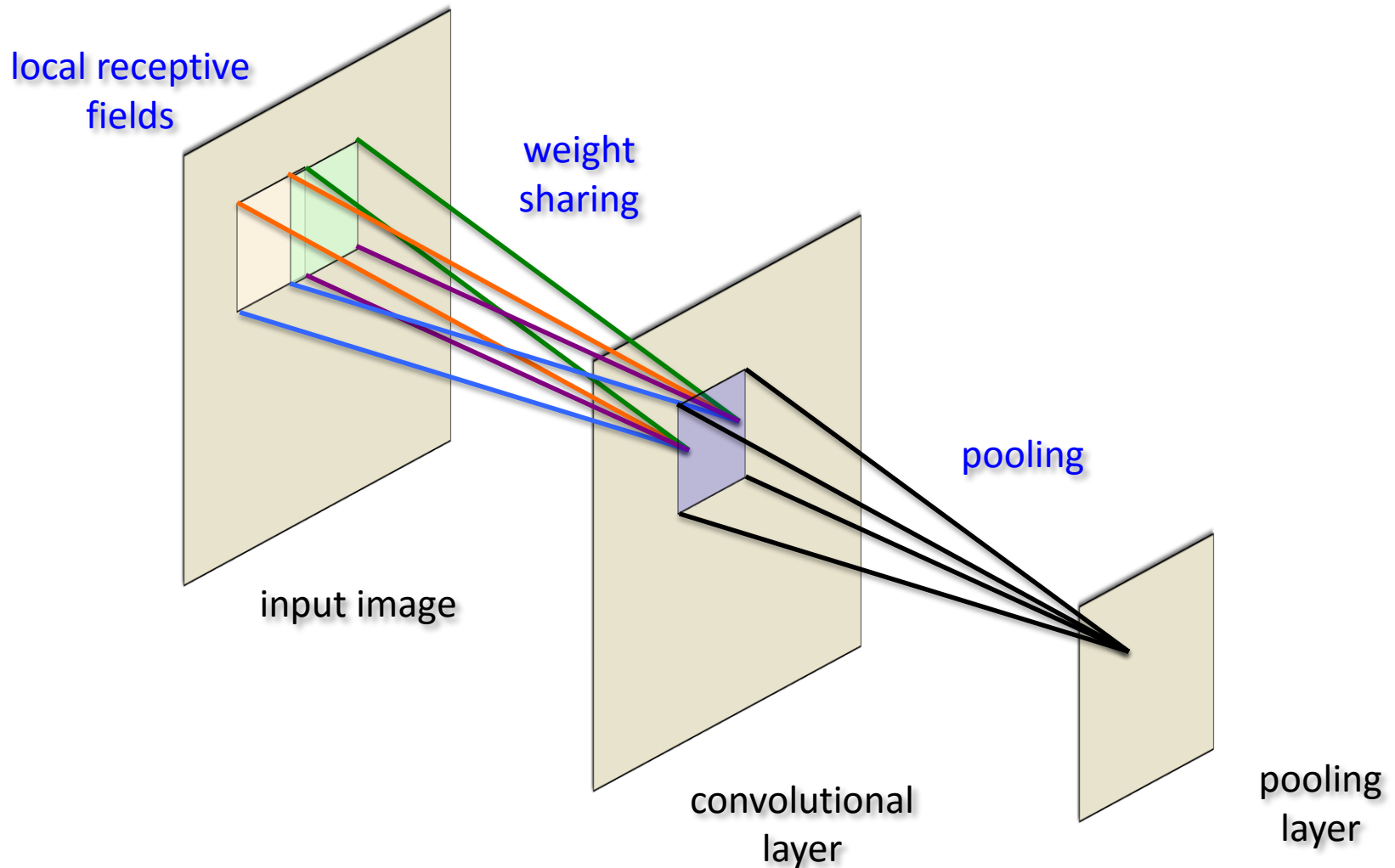
- **Convolution**: feature detector
- **Max-pooling**: local translation invariance

determines the future state of a certain cell in the grid by the inputs and past states of its local neighbors

Size of state-to-state convolutional kernel for capturing of spatiotemporal motion patterns



Convolutional and pooling layers



NN and Fully-connected Recurrent NN

Feed-forward NN

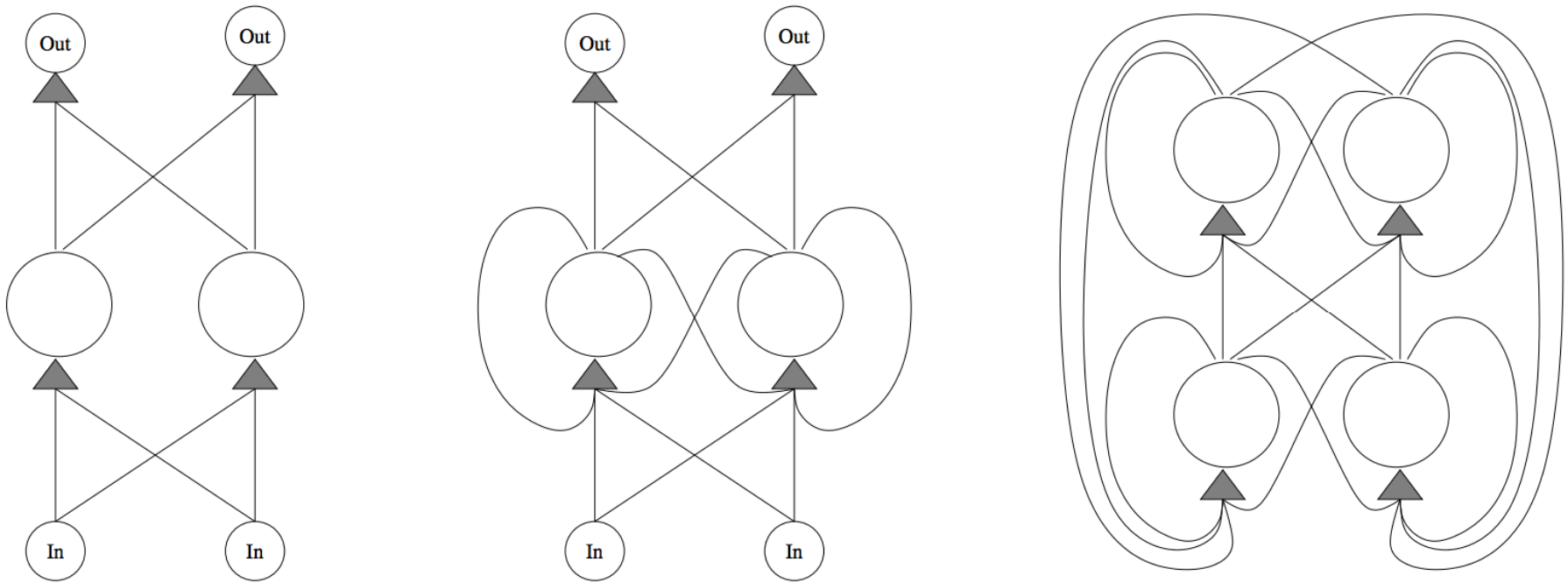


Figure 1.1: Left: Feed-forward neural network. Middle: Layered network with an input layer, a fully recurrent hidden layer and an output layer. Right: Fully connected recurrent network.

From RNN to LSTM

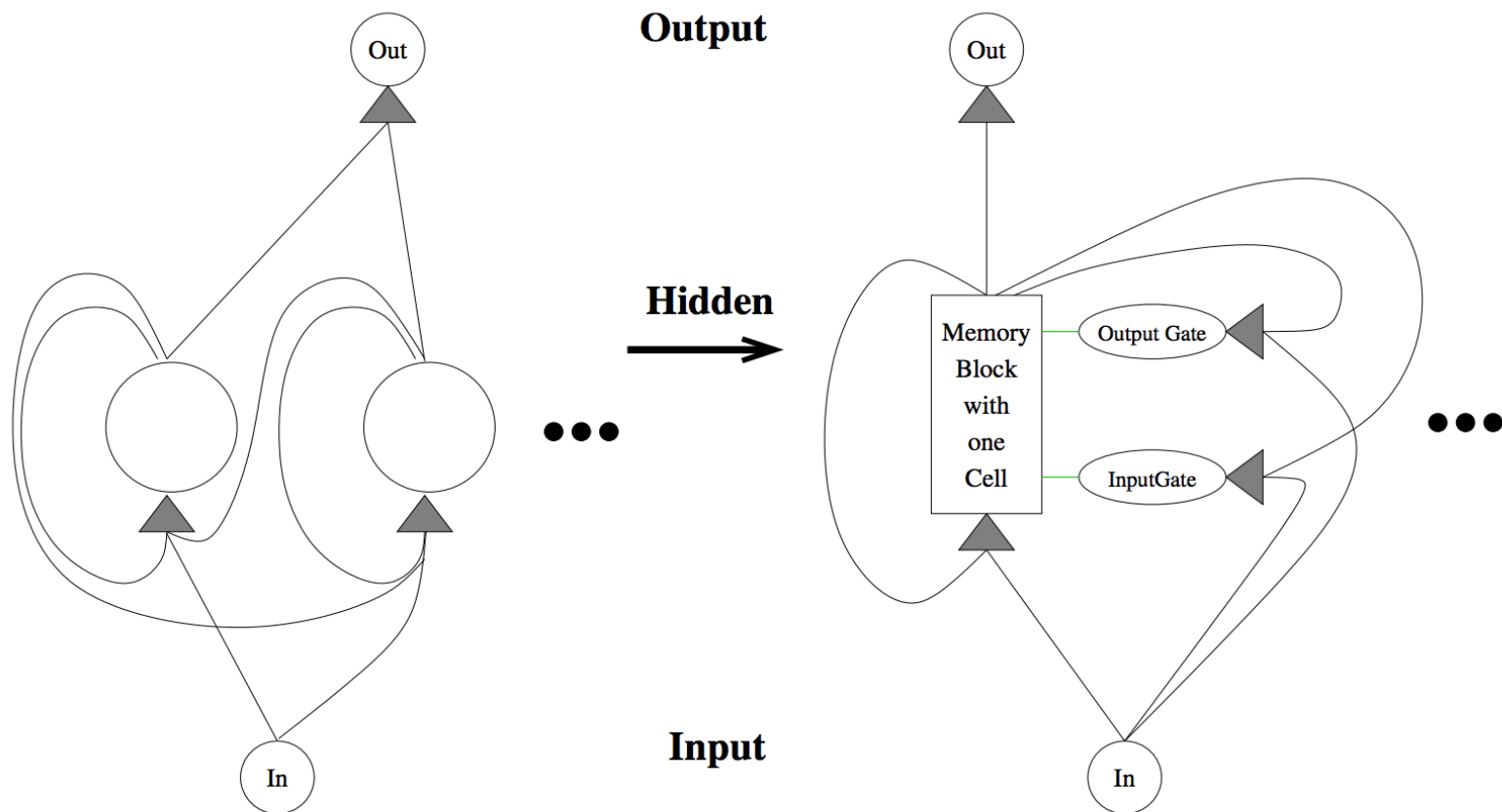
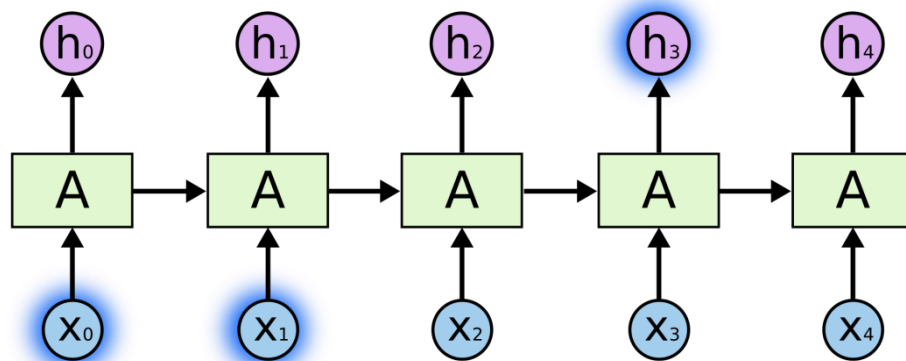


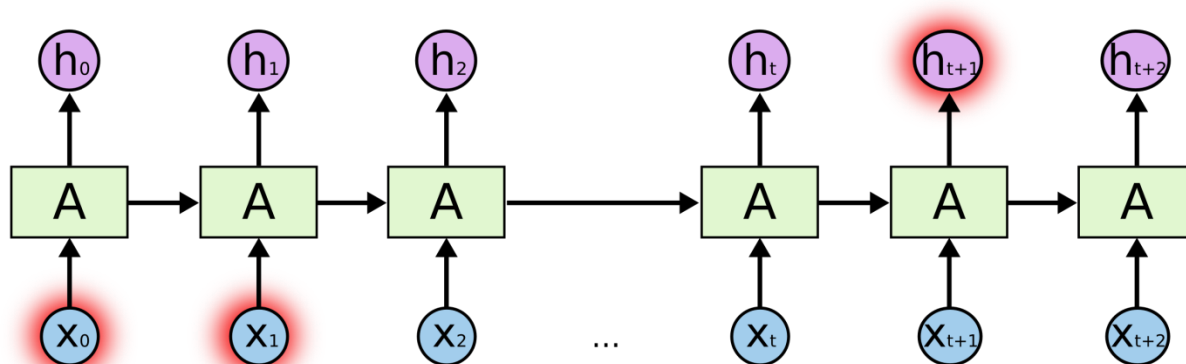
Figure 2.1: Left: RNN with one fully recurrent hidden layer. Right: LSTM network with memory blocks in the hidden layer (only one is shown).

Dependencies between events in RNNs

- Short-term dependencies:

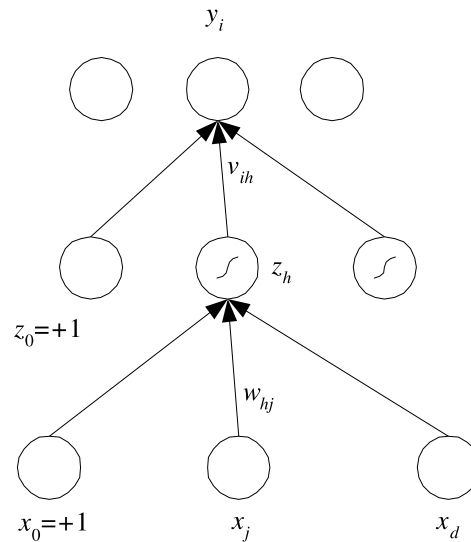


- Long-term dependencies:



Ordinary hidden units in multilayered networks

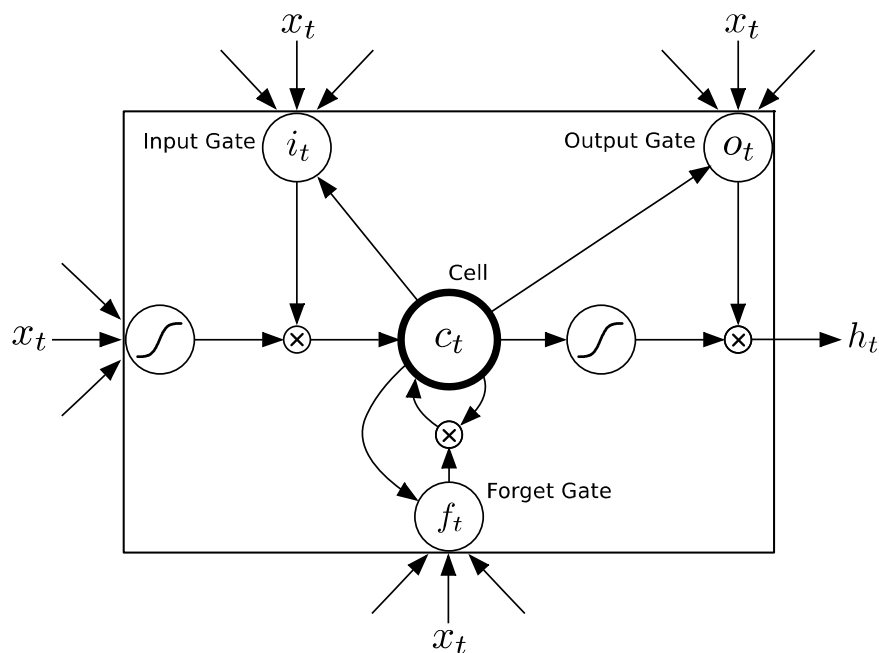
- Nonlinear function (e.g., sigmoid or hyperbolic tangent) of weighted sum

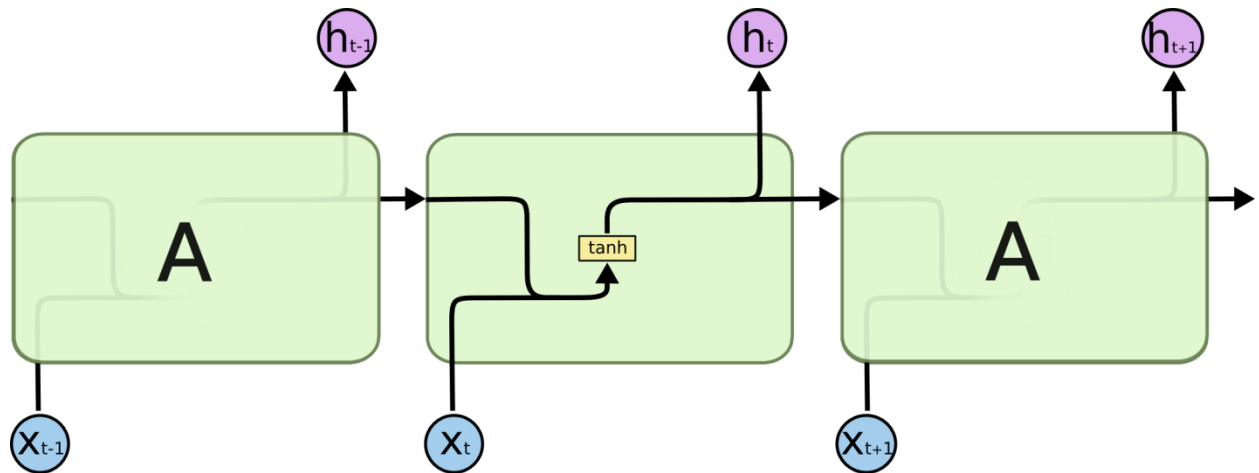


- RNNs, like deep multilayered networks, suffer from the **vanishing gradient problem**

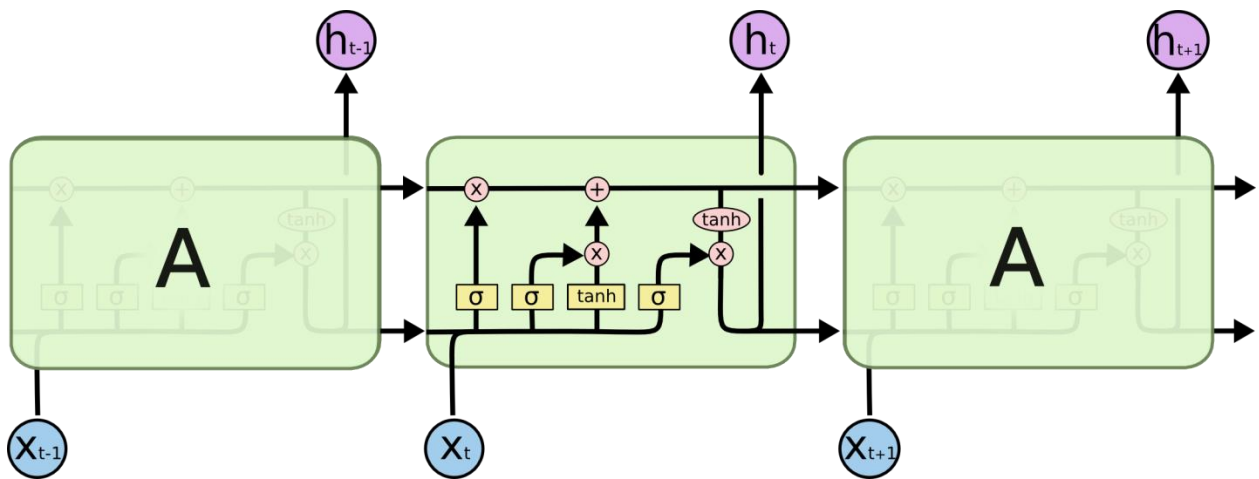
LSTM units

- LSTM units, which are essentially subnets, can help to learn **long-term dependencies** in RNNs
- 3 gates in an LSTM unit: **input gate**, **forget gate**, **output gate**





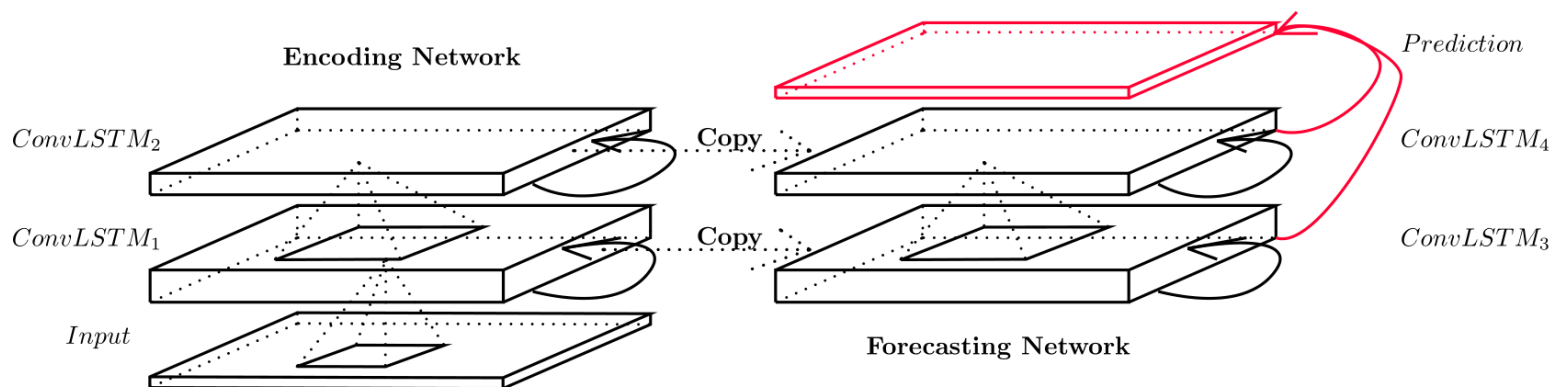
RNNs with ordinary unit



RNNs with LSTM units

Encoding-forecasting ConvLSTM network

- Last states and cell outputs of encoding network become initial states and cell outputs of forecasting network
- **Encoding network** compresses the input sequence into a hidden state tensor
- **Forecasting network** unfolds the hidden state tensor to make prediction



ConvLSTM governing equations

Accumulator of
state
information

Memory
cell

Inputs

input gate

$$i_t = \sigma(W_{xi} * \mathcal{X}_t + W_{hi} * \mathcal{H}_{t-1} + W_{ci} \circ \mathcal{C}_{t-1} + b_i)$$

forget gate

$$f_t = \sigma(W_{xf} * \mathcal{X}_t + W_{hf} * \mathcal{H}_{t-1} + W_{cf} \circ \mathcal{C}_{t-1} + b_f)$$

Cell outputs

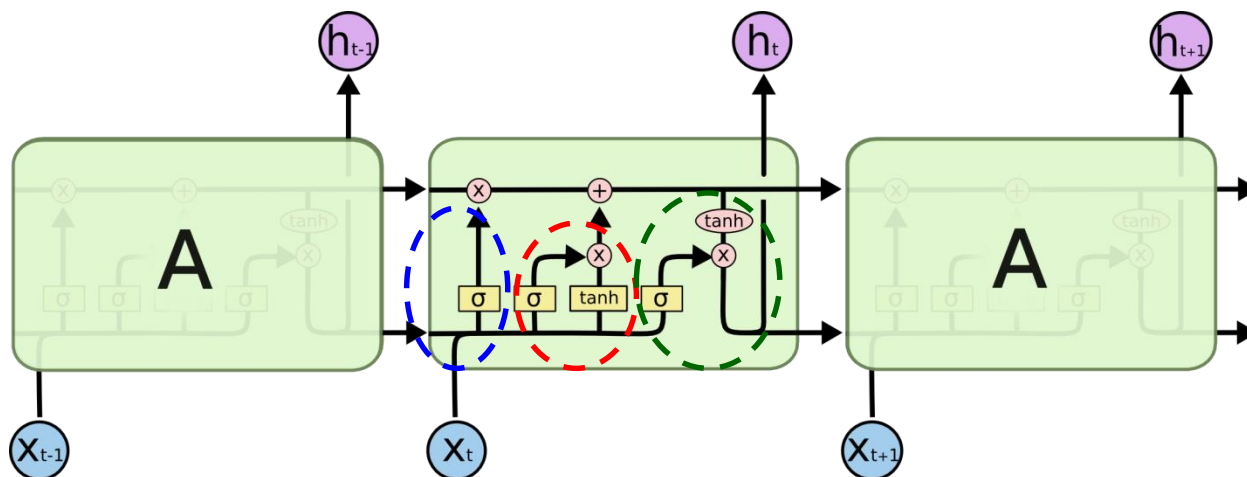
$$\mathcal{C}_t = f_t \circ \mathcal{C}_{t-1} + i_t \circ \tanh(W_{xc} * \mathcal{X}_t + W_{hc} * \mathcal{H}_{t-1} + b_c)$$

output gate

$$o_t = \sigma(W_{xo} * \mathcal{X}_t + W_{ho} * \mathcal{H}_{t-1} + W_{co} \circ \mathcal{C}_t + b_o)$$

Hidden states

$$\mathcal{H}_t = o_t \circ \tanh(\mathcal{C}_t)$$



Training and preprocessing of radar echo dataset

- 97 days in 2011-2013 with high radar intensities
- Preprocessing of radar maps:
 - Pixel values normalized
 - 330 x 330 central region cropped
 - Disk filter applied
 - Resized to 100 x 100
 - Noisy regions removed

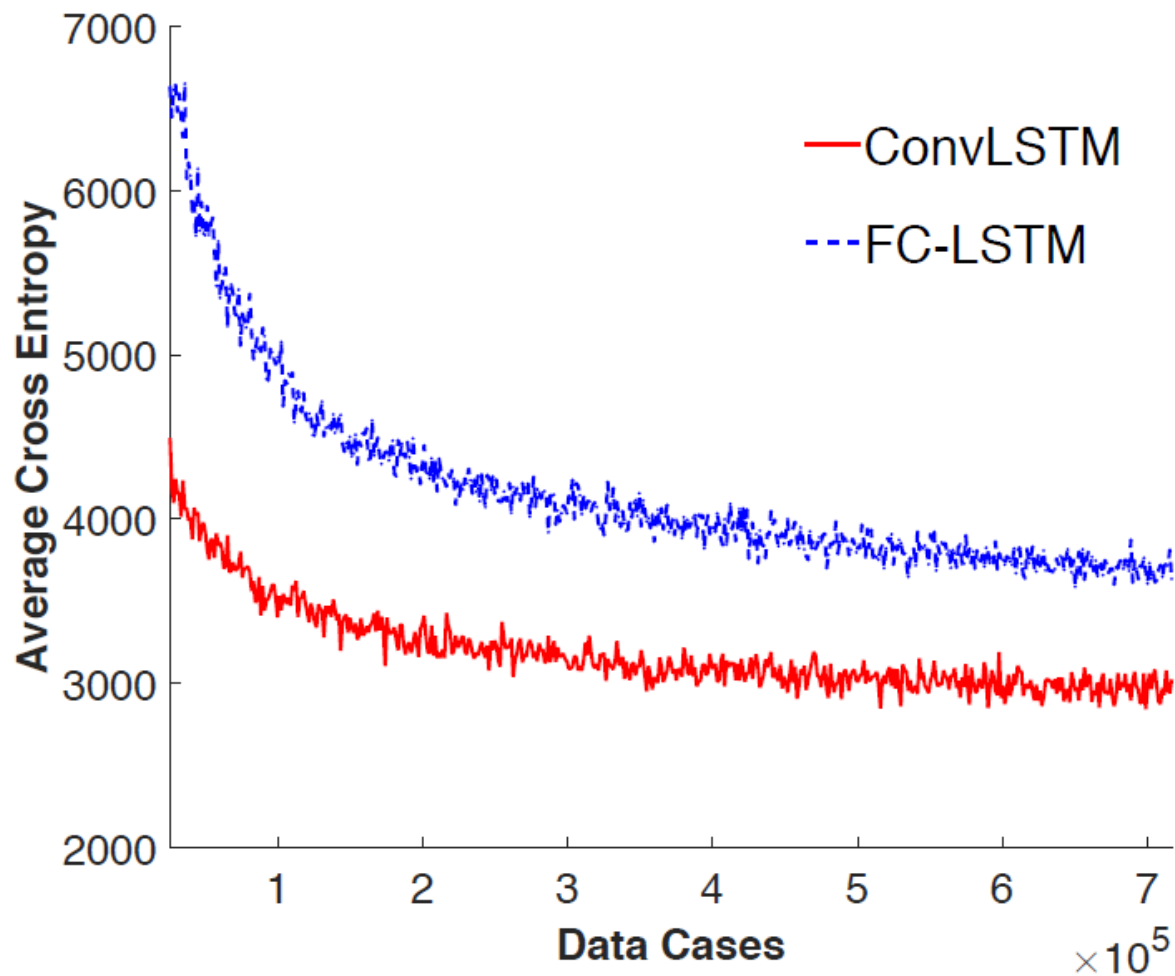
Data splitting

- 240 radar maps (a.k.a. frames) per day partitioned into **six 40-frame blocks**
- Random data splitting:
 - **Training**: 8148 sequences
 - **Validation**: 2037 sequences
 - **Testing**: 2037 sequences
- 20-frame sequence :
 - **Input sequence**: 5 frames
 - **Output sequence**: 15 frames (i.e., 6-90 minutes)

Comparison of performance

- **ConvLSTM network:**
 - 2 ConvLSTM layers, each with 64 units and 3 x 3 kernels
- **Fully connected LSTM (FC-LSTM) network:**
 - 2 FC-LSTM layers, each with 2000 units
- **ROVER:**
 - Optical flow estimation
 - 3 variants (**ROVER1**, **ROVER2**, **ROVER3**) based on different initialization schemes

Comparison of ConvLSTM and FC-LSTM



the loss of entropy for ConvLSTM decreases faster than FC-LSTM across all the data cases

➔ a better matching with training datasets

Comparison based on 5 performance metrics

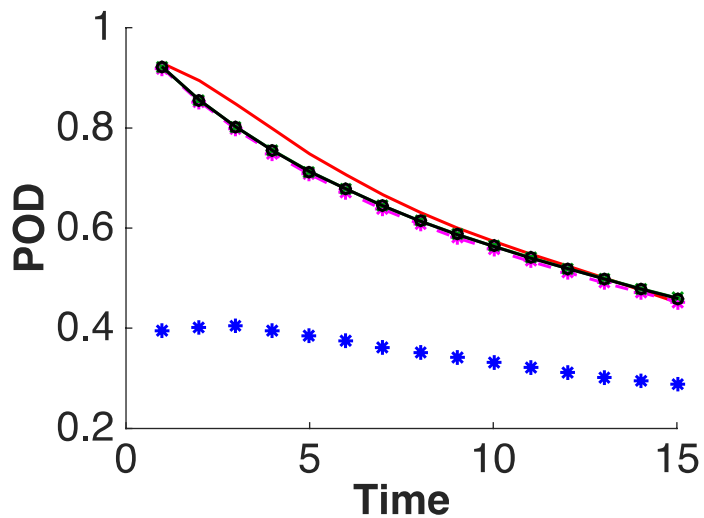
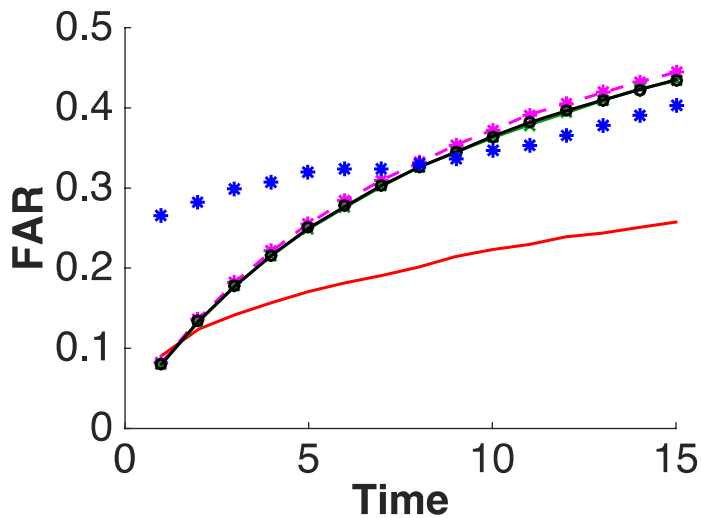
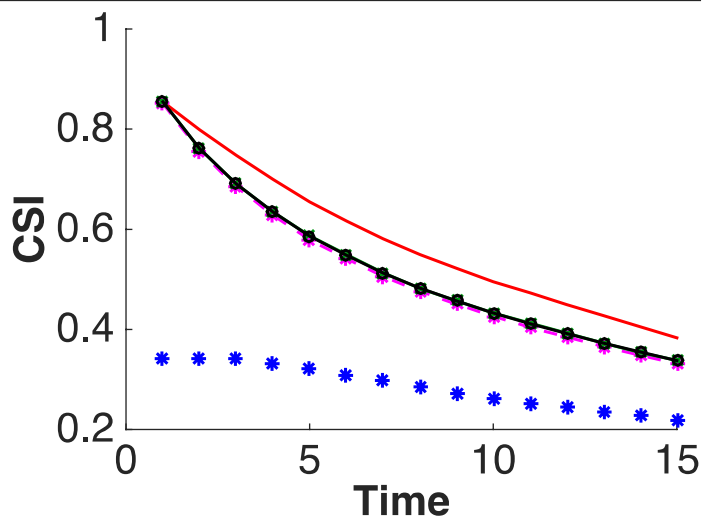
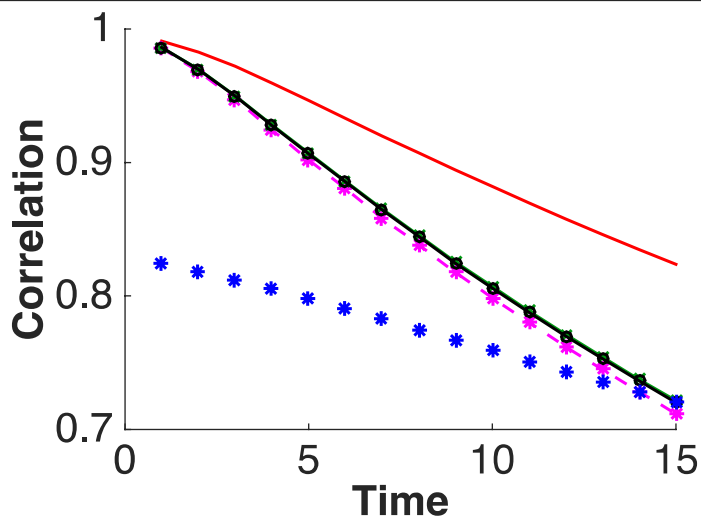
- Rainfall mean squared error (Rainfall-MSE)
- Critical success index (CSI)
- False alarm rate (FAR)
- Probability of detection (POD)
- Correlation

Model	Rainfall-MSE	CSI	FAR	POD	Correlation
ConvLSTM(3x3)-3x3-64-3x3-64	1.420	0.577	0.195	0.660	0.908
Rover1	1.712	0.516	0.308	0.636	0.843
Rover2	1.684	0.522	0.301	0.642	0.850
Rover3	1.685	0.522	0.301	0.642	0.849
FC-LSTM-2000-2000	1.865	0.286	0.335	0.351	0.774

Threshold = 0.5 mm/h

Prediction accuracy vs prediction horizon

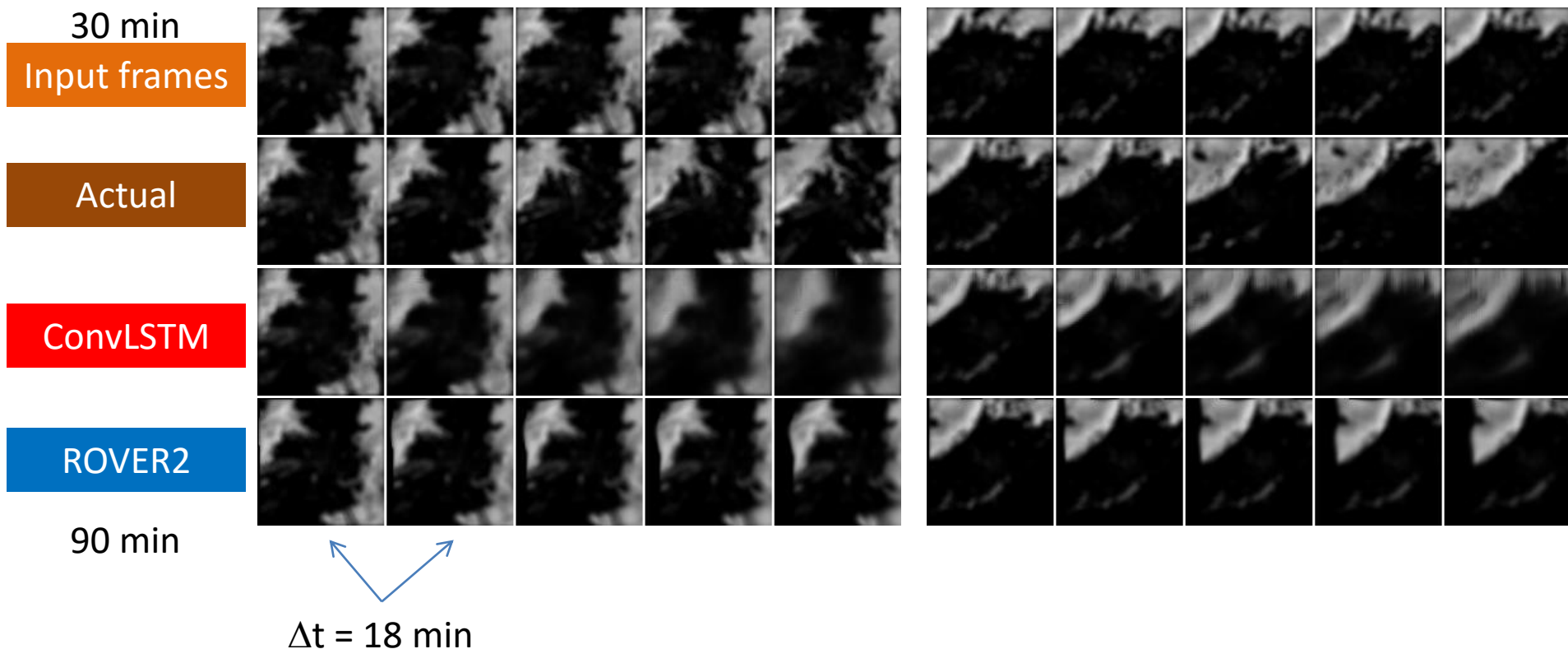
— ConvLSTM * ROVER1 * ROVER2 * ROVER3 * FC-LSTM



Different parameters are used in ROVER1,2,3 optical flow estimators

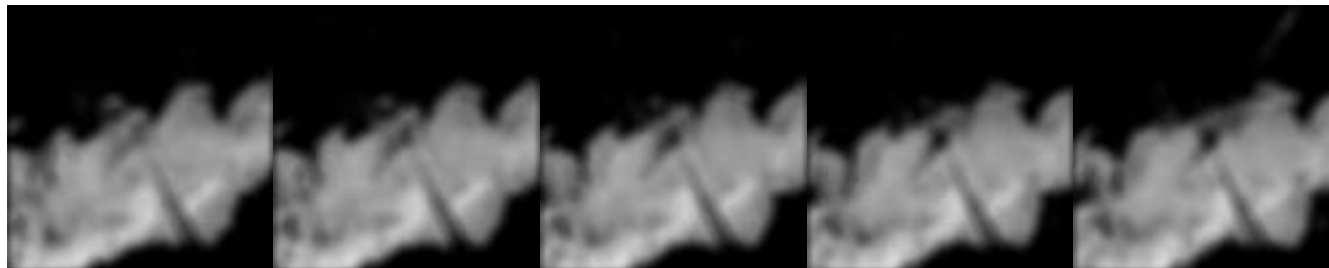
Two squall line cases

- Radar location (HK) at center (~ 250 km in x- and y- directions)
- 5 input frames are used and a total of 15 frames (i.e. T+90 min) in forecasts



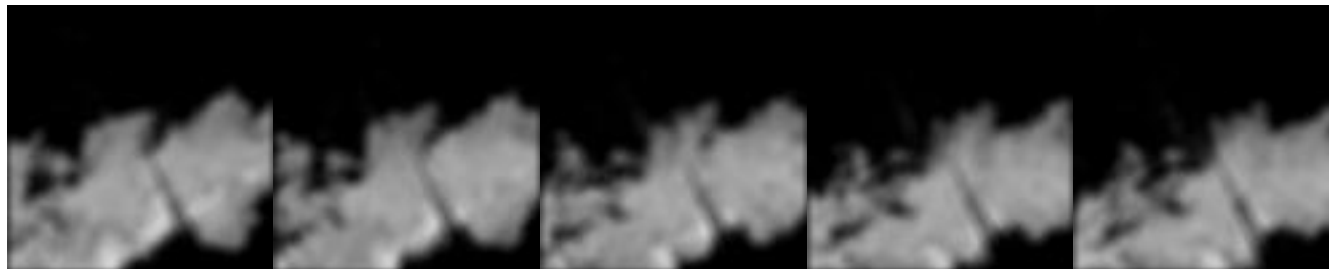
30 min

Input frames



90 min

Actual



ConvLSTM

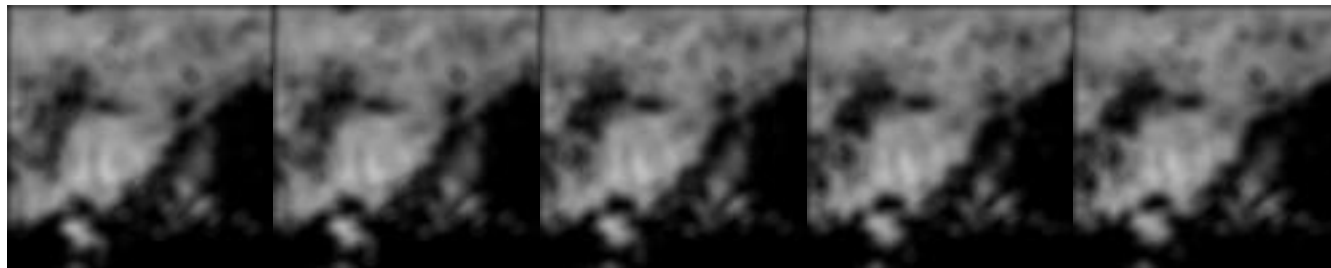


ROVER2



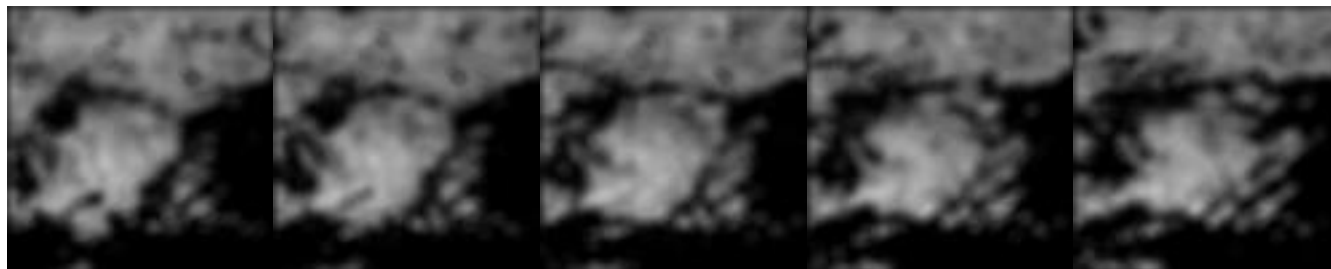
30 min

Input frames

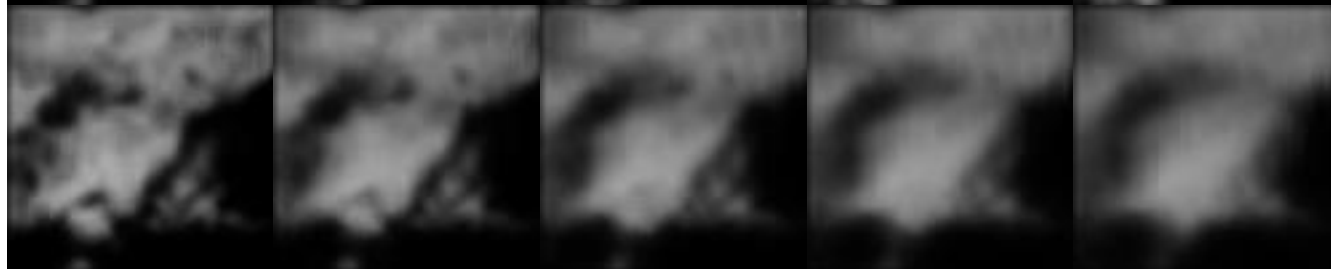


90 min

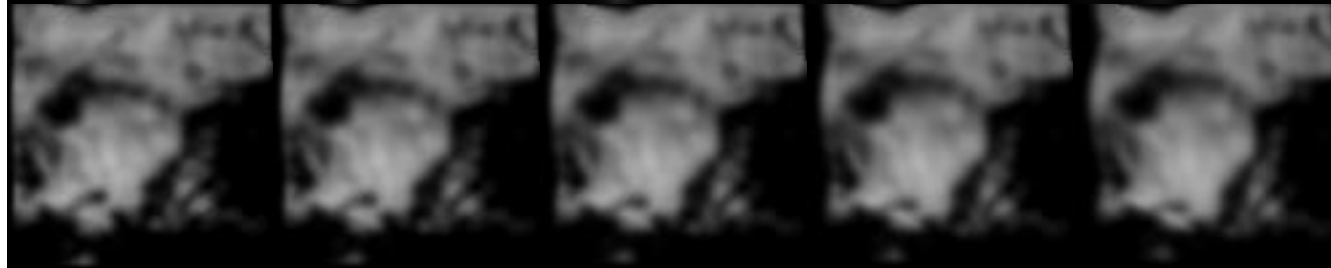
Actual



ConvLSTM



ROVER2



Ongoing Development

- Longer training dataset (~ 10 years data)
- Adaptive learning to cater for multiple time scale processes
- Optimizing performance for higher rainfall intensity based on different convolutional and pooling strategies
- Extend learning process to extract stochastic characteristics of radar echo time sequence, features of convective development from mesoscale/fine-scale NWP models